

# for Introductory Physics

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## Answers

1. CHOICE D: We are given  $x - 1 = 2$ . To solve for  $x$ , add 1 to both sides of the equation:
 
$$\begin{array}{r} x - 1 = 2 \\ + 1 = + 1 \\ \hline x = 3 \end{array}$$
 so  $x + 1 = (3 + 1) = 4$
  
2. CHOICE B: volume = "  $R^2 h = (3)(2 \text{ cm})^2 (5 \text{ cm}) = 60 \text{ cm}^3$
  
3. CHOICE C: If  $x = 3$  then  $x^2 + 3 = 3^2 + 3 = 9 + 3 = 12$
  
4. CHOICE C: The area is 8 entire squares plus  $0.8 + 0.4 + 0.9 + 0.1 + 0.5$  squares which is 10.7 squares. Each square has an area of so the total area is about 53.5.
  
5. CHOICE A:  $\frac{(-2)(-6)}{\text{-----}} = \frac{12}{\text{-----}} =$ 

$$(2xy^3)^3 = 2^3 x^3 (y^3)^3 = 8x^3 y^9$$
  
7. CHOICE A:  $(2x - 1)(4x + 1) = 2x(4x + 1) + (-1)(4x + 1)$ 

$$= 8x^2 + 2x - 4x - 1$$

$$= 8x^2 - 2x - 1$$
  
8. CHOICE A:  $\frac{4^n 10^{\#15}}{\text{-----}}$       #15+12      #3      #4

9. CHOICE D: A common denominator is  $xy$ . Multiply the first term by  $\frac{x}{x}$  to get

$$\frac{x^2 y}{xy} + \frac{x}{y} = \frac{x^2 y + x}{xy}$$

10. CHOICE C: This is the difference between two squares.

$$x^2 - 100 = (x - 10)(x + 10)$$

11. CHOICE A:  $(5 \cdot 10^8)(6 \cdot 10^{-12}) = 30 \cdot 10^{8-12} = 30 \cdot 10^{-4} = 3 \cdot 10^{-3}$

12. CHOICE A:  $(2x + 3) - (x - 2) = 2x + 3 - x + 2 = x + 5$

13. CHOICE C:  $x^2 + 2x + 2 = (x + 1)^2 + 1$

14. CHOICE C: Let  $x$  be the number. "Of" means multiply. "is" means equals.

$$\frac{1}{3}(x) = 8$$

Multiply both sides by 3:

$$x = 24$$

$$\frac{1}{4}(24) = 6$$

15. CHOICE A:  $(-3xy - (-2)^3) - (-8)(-5) = -10$

16. CHOICE E:  $25 \text{ m} = (25 \text{ m})(3 \text{ feet})$

17. CHOICE C:  $(x^2 - 3x + 2) - (3x^2 - 5x - 1)$

$$= x^2 - 3x + 2 - 3x^2 + 5x + 1$$

$$= -2x^2 + 2x + 3$$

18. CHOICE D:  $\frac{2x}{3y} - \frac{9y}{4x^2} = \frac{2x^3 - 9y^2}{3y \cdot 4x^2} = \frac{2x^3 - 9y^2}{12x^2 y}$



29. CHOICE D:  $10(-2) = -20$  and  $11 = 11$  so  $-20 + 11 = -9$

$$\frac{-20}{5} + \frac{11}{5} = \frac{-9}{5}$$

30. CHOICE A: The graphs of  $x - 2y = 6$  and  $x + y = -3$  intersect at the values of  $x$  and  $y$  that satisfy both equations. To get these, solve the two equations.

6. Substitute into the second equation:

$$(2y + 6) + y = -3$$

$$= 3y + 6 = -3$$

Subtract 6 from both sides:

$$3y + 6 = -3$$

$$-6 \quad -6$$

$$3y = -9$$

Divide both sides by three:

$$y = -3$$

$$3 \quad 3$$

$$y = -3$$

31. CHOICE B:  $\frac{2x^2 + 3x - 2}{x^2 - 4} = \frac{(2x - 1)(x + 2)}{(x - 2)(x + 2)}$

$$\frac{2x - 1}{x - 2} = \frac{2x - 1}{x - 2}$$

32. CHOICE B:  $\sqrt{-27} = -3i$  because  $(-3i)(-3i)(-3i) = -27i$ . Roots can be negative.

33. CHOICE A: As  $x$  becomes very large and positive,  $y$  becomes very large because the term  $x^3$  increases much faster than that in  $x$ . The same is true as  $x$  becomes very negative. Also recall an equation of the form  $ax^2 + bx + c$  is a parabola.

34. CHOICE D: Recall that  $\log_3(9) = 2$  means...

$$\log_3(x + 1) = 2 \text{ means } x + 1 = 9$$

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$$= 6w + 6 = 90$$

$$\quad - 6 \quad - 6$$

$$\text{-----}$$

$$6w = 84$$

$$\text{---} \quad \text{---}$$

$$6 \quad 6$$

$$w = 14$$

56. CHOICE A:  $4(s + 2) = (4 \times s) + (4 \times 2) = 4s + 8$

57. CHOICE A:  $3/4 \times 1/7 = \frac{3}{4} \times \frac{1}{7} = \frac{3 \times 1}{4 \times 7} = \frac{3}{28} = \frac{17}{28}$

58. CHOICE B: Subtract one from both sides:

$$1 - 5x < 3$$

$$- 1 \quad - 1$$

$$\text{-----}$$

$$- 5x < 2$$

Divide both sides by -5, and remember to switch the sign of the inequality because we are dividing by a negative number:

$$- 5x < 2$$

$$\text{-----} \quad \text{---}$$

$$- 5 \quad - 5$$

$$x > - 2 / 5$$

59. CHOICE B: The function has an absolute minimum at  $x = 1$ , the lowest point on the graph between 0 and 4. The other low point at  $x = 3$  is a "local minimum."

60. CHOICE A:  $3^2 + 4^2 = D^2 = 25$  so  $D = 5$ .

61. CHOICE B:  $(2\sqrt{3})(3\sqrt{6}) = 6\sqrt{18} = 6\sqrt{(2)(9)} =$   
 $6\sqrt{9}\sqrt{2} = (6)(3)\sqrt{2} = 18\sqrt{2}$

62. CHOICE B:  $1 - \sin^2 \theta = \cos^2 \theta$  (a trigonometric identity).

63. CHOICE A:  $f(x) = \cos(3x)$ , then  $f(\pi/6) = \cos(\pi/2) = 0$ .



64. CHOICE A: The circumference of a circle is  $2\pi R$ .
65. CHOICE E: The sine curve has a y-intercept at zero, increases as  $x$  increases to  $\pi/2$  and decreases as  $x$  decreases to  $-\pi/2$ .
66. CHOICE E:  $\csc \theta = 1/\sin \theta$  and  $\tan \theta = \sin \theta / \cos \theta$ , so  
 $\sin \theta \tan \theta \csc^2 \theta = \sin \theta (\sin \theta / \cos \theta) (1/\sin^2 \theta) = 1/\cos \theta = \sec \theta$ .
67. CHOICE B:  $\tan \theta = \sin \theta / \cos \theta$ , and  $\cos(-\pi/2)$  is zero. A zero in the denominator renders the expression undefined.
68. CHOICE E: The area of a circle is  $\pi R^2$ .
69. CHOICE B: the sum of the angles in a triangle add up to 180 degrees.
70. CHOICE C: Taking the slope between  $x = 0$  and  $x = 5$ , we see that:

$$\text{slope} = \frac{\text{change in } y}{\text{change in } x} = \frac{20 - 5}{5 - 0} = \frac{15}{5} = 3$$

71. CHOICE E:  $\frac{100 \text{ km}}{1 \text{ minute}} = \frac{100 \text{ km} \cdot 5 \text{ miles}}{8 \text{ km} \cdot 60 \text{ seconds}}$   
 $= \frac{500 \text{ miles}}{480 \text{ seconds}} = 1 \frac{\text{mile}}{\text{second}}$