## Philadelphia Area Number Theory Seminar

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## Quadratic Identities and Maass Waveforms

**Abstract**: Andrews, Dyson, and Hickerson (ADH) studied the Fourier coe cients of the function

$$(q) = 1 + \frac{\cancel{x}}{(1+q)(1+q^2)} \frac{q^{n(n+1)=2}}{(1+q^n)};$$

where is a function that appears in the work of Ramanujan. They prove, among other things, that, for m>0 and m=1 mod 24, that these Fourier coeficients are given by

$$T(m) = \# \begin{pmatrix} (\\ equivalence classes [(x;y)] \text{ of solutions to} \\ x^2 & 6y^2 = m \text{ with } x + 3y & 1 \text{ mod } 12 \\ (\\ equivalence classes [(x;y)] \text{ of solutions to} \\ x^2 & 6y^2 = m \text{ with } x + 3y & 5 \text{ mod } 12 \end{pmatrix}$$

Cohen showed that

$$_{0}() = y^{1=2} \times T(n)e^{2 inx=24} K_{0} \frac{2 jnjy}{24}$$

is a Maass waveform on  $_0(2)$ . Zweger was able to place  $_0($  ) in a larger framework of inde nite theta functions.

In this talk, I will discuss the problem of placing quadratic identities arising in the work of ADH into a modular framework. This is joint work, in progress, with Larry Rolen.

## Wednesday, February 14, 2018, 2:40 { 4:00 PM

Bryn Mawr College, Department of Mathematics
Park Science Center **328** Tea and refreshments at 2:20PM in Park 339